

T. HOEFLER, T. BEN-NUN

Optimizing and Benchmarking Large-Scale Deep Learning

Machine Learning Day at ISC'19, Frankfurt, Germany

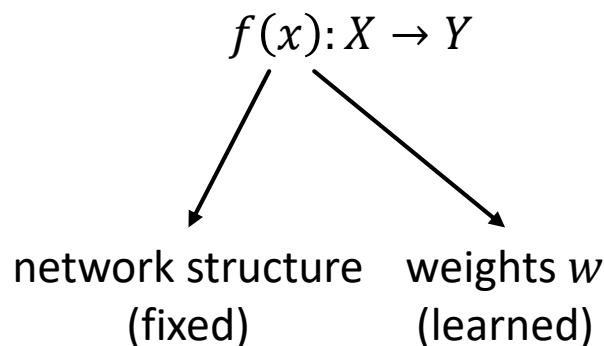
WITH CONTRIBUTIONS FROM DAN ALISTARH, YOSUKE OYAMA, CEDRIC RENGLI, AND OTHERS AT SPCL, IST AUSTRIA, AND TOKYO TECH



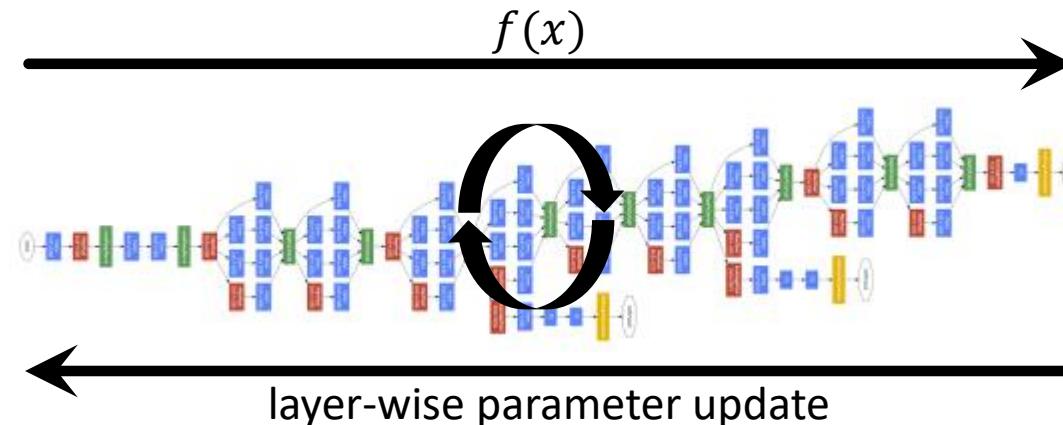
A brief theory of supervised deep learning (minibatch SGD)



labeled samples $x \in X \subset \mathcal{D}$



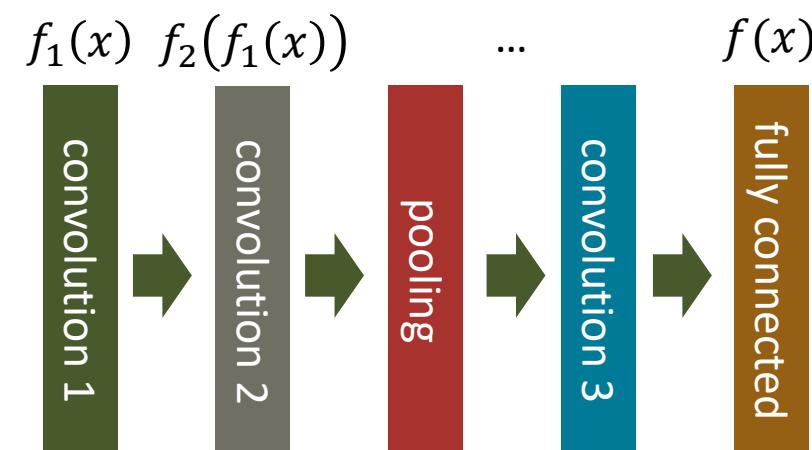
$$w^* = \operatorname{argmin}_{w \in \mathbb{R}^d} \mathbb{E}_{x \sim \mathcal{D}} [\ell(w, x)]$$



Cat	0.54	Cat	1.00
Dog	0.28	Dog	0.00
Airplane	0.07	Airplane	0.00
Horse	0.33	Horse	0.00
Banana	0.02	Banana	0.00
Truck	0.02	Truck	0.00

label domain Y true label $l(x)$

$$f(x) = f_n \left(f_{n-1} \left(f_{n-2} \left(\dots f_1(x) \dots \right) \right) \right)$$

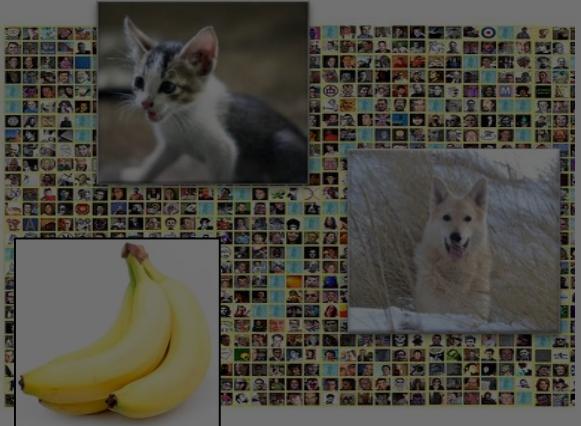


$$\ell_{sq}(w, x) = (f(x) - l(x))^2$$

$$\ell_{0-1}(w, x) = \begin{cases} 0 & f(x) = l(x) \\ 1 & f(x) \neq l(x) \end{cases}$$

$$\ell_{ce}(w, x) = - \sum_i l(x)_i \cdot \log \frac{e^{f(x)_i}}{\sum_k e^{f(x)_k}}$$

A brief theory of supervised deep learning (minibatch SGD)



\geq TBs of random access

100MiB-26GiB and beyond

$$f(x) = f_n \left(f_{n-1} \left(f_{n-2} \left(\dots f_1(x) \dots \right) \right) \right)$$

22k-millions

(fixed)

(learned)

$$w^* = \operatorname{argmin}_{w \in \mathbb{R}^d} \mathbb{E}_{x \sim \mathcal{D}} [\ell(w, x)]$$

volution 1

volution 2

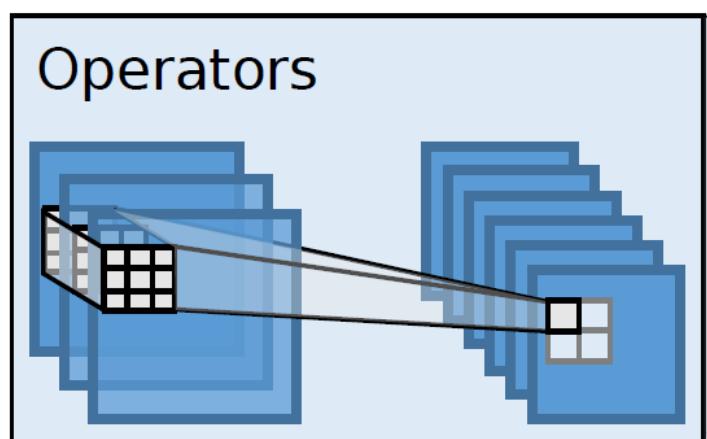
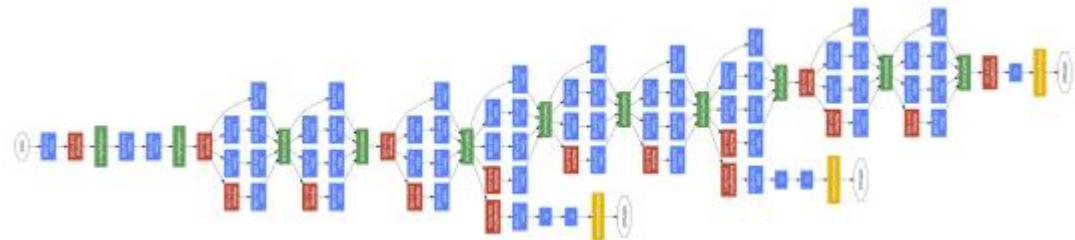
pooling

volution 3

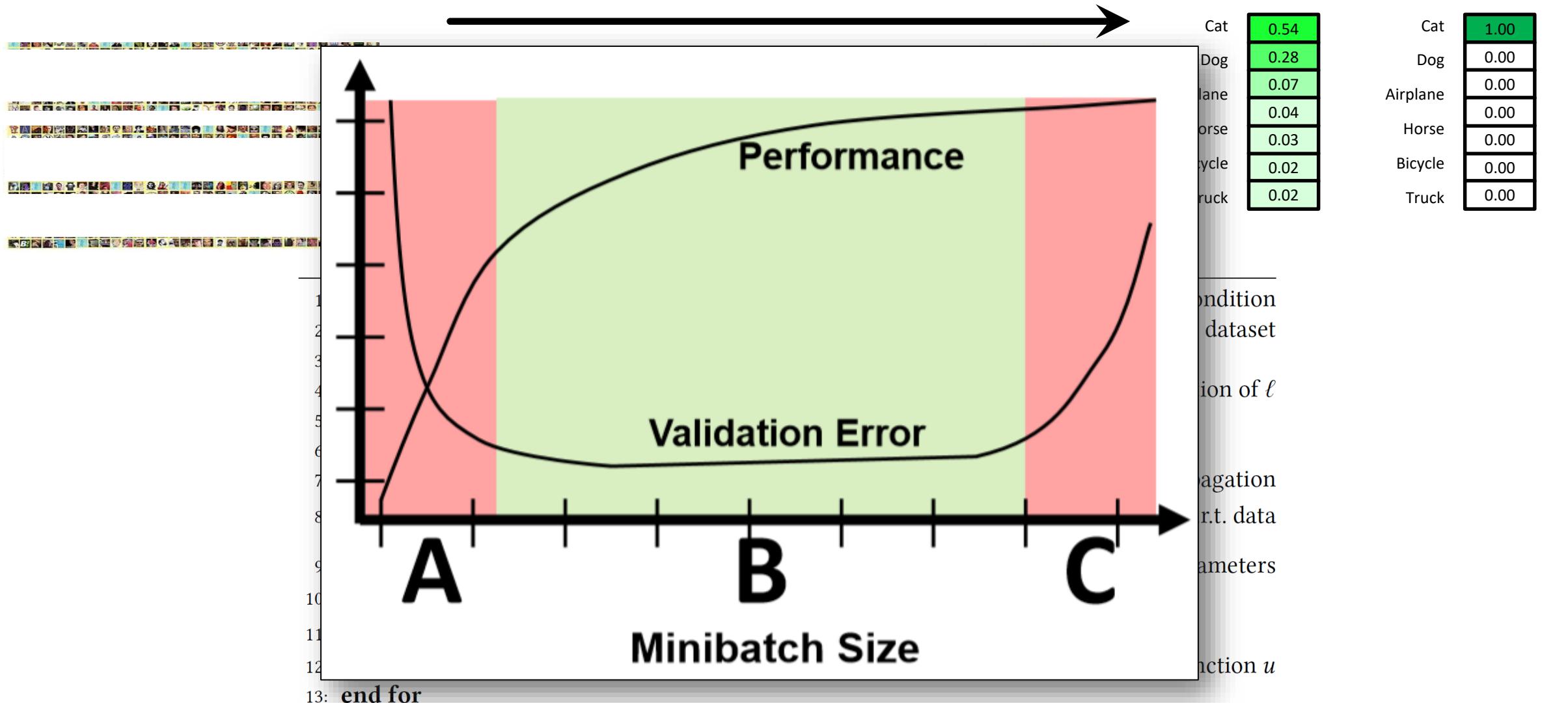
connected

$$\ell_{ce}(w, x) = - \sum_i l(x)_i \cdot \log \frac{e^{f(x)_i}}{\sum_k e^{f(x)_k}}$$

Computational Principles



Minibatch Stochastic Gradient Descent (SGD)



Microbatching (μ -cuDNN) – how to implement layers best in practice?



- In cuDNN there are ~16 convolution implementations
- Performance depends on temporary memory (workspace) size
- Key idea: segment minibatch into microbatches, reuse

Microbatching Strategy

- How to choose microbatches?

none (undivided)

$$T(b) = \min \left\{ T_{\mu}(b), \min_{b' \in 1, 2, \dots} \right\}$$

powers-of-two only

Dynamic Programming

any (unrestricted)

$$\min T = \sum_{k \in \mathcal{K}} \sum_{c \in C_k}$$

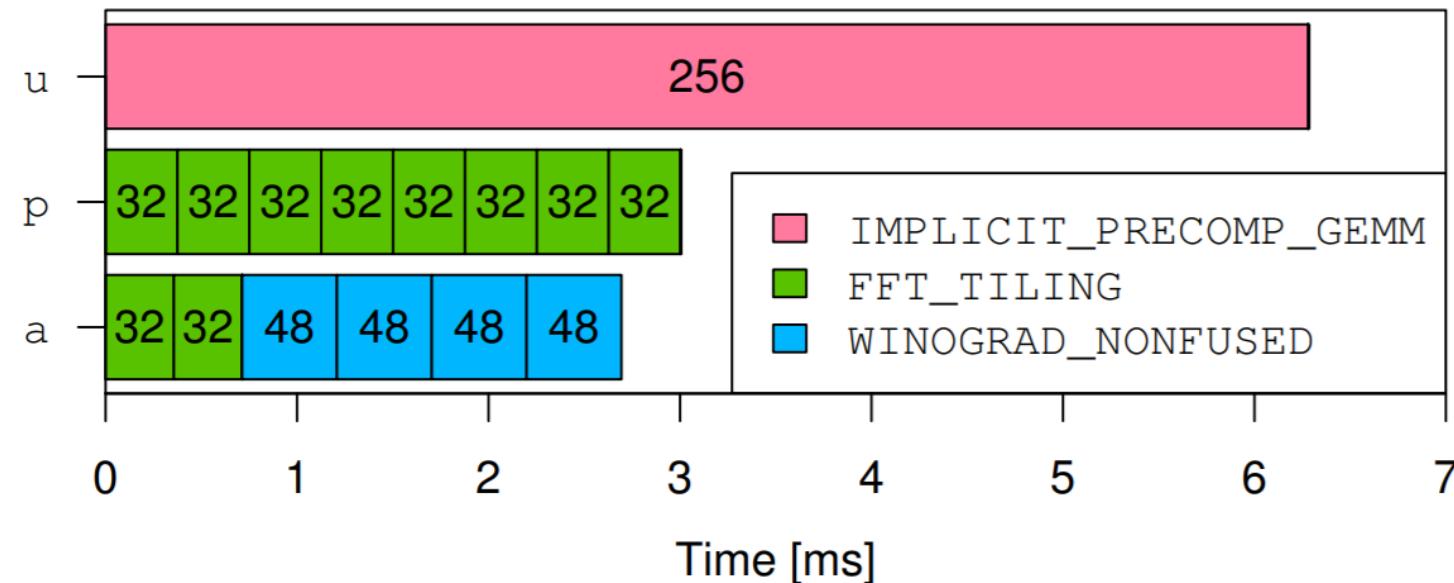
subject to

$$\sum_{k \in \mathcal{K}} \sum_{c \in C_k}$$

$$\sum_{c \in C_k}$$

$$x_{k,c} \in \{0, 1\} \quad (\forall k \in \mathcal{K}, \forall c \in C_k)$$

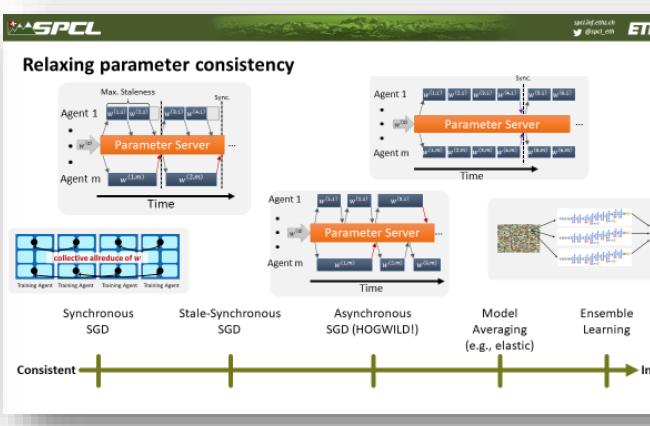
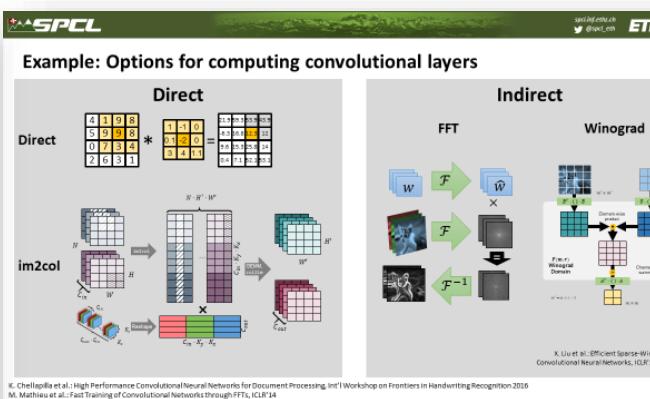
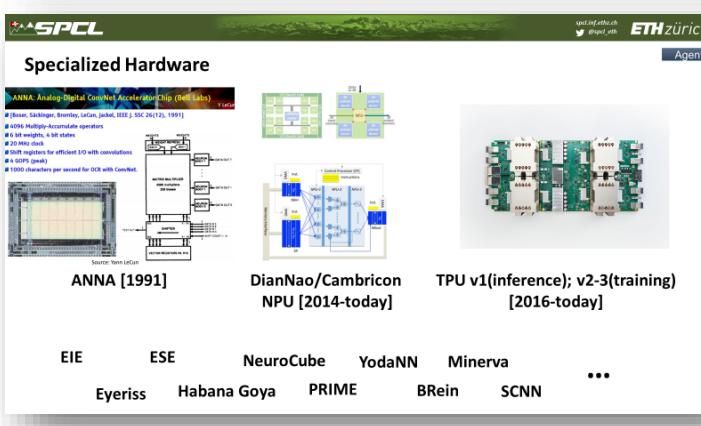
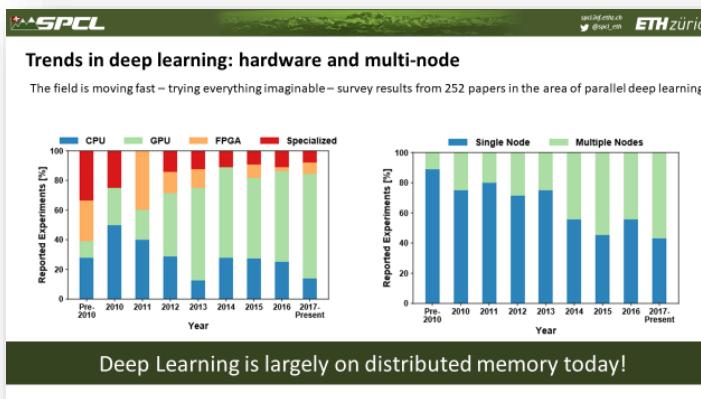
Fast (up to 4.54x faster on DeepBench)



Integer Linear Programming (Space Sharing)

Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis

- <https://www.arxiv.org/abs/1802.09941>



Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis

TAL BEN-NUN* and TORSTEN Hoeffler, ETH Zurich

Deep Neural Networks (DNNs) are becoming an important tool in modern computing applications. Accelerating their training is a major challenge and techniques range from distributed algorithms to low-level circuit design. In this survey, we describe the problem from a theoretical perspective, followed by approaches for its parallelization. Specifically, we present trends in DNN architectures and the resulting implications on parallelization strategies. We discuss the different types of concurrency in DNNs; synchronous and asynchronous stochastic gradient descent; distributed system architectures; communication schemes; and performance modeling. Based on these approaches, we extrapolate potential directions for parallelism in deep learning.

CCS Concepts: • General and reference → Surveys and overviews; • Computing methodologies → Neural networks; Distributed computing methodologies; Parallel computing methodologies; Machine learning;

Additional Key Words and Phrases: Deep Learning, Distributed Computing, Parallel Algorithms

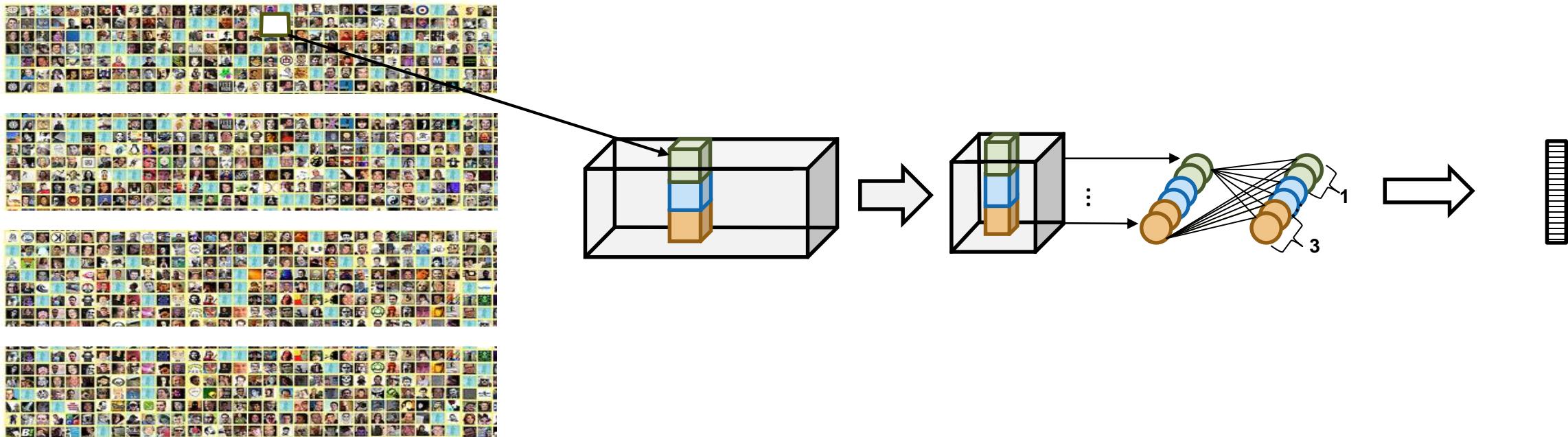
ACM Reference format:

Tal Ben-Nun and Torsten Hoefer. 2018. Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis. 60 pages.

1 INTRODUCTION

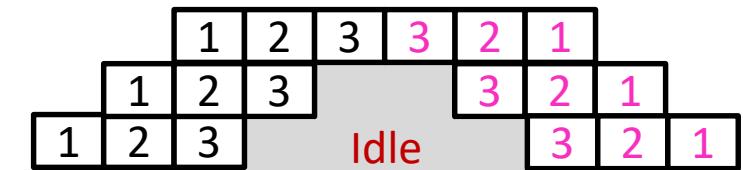
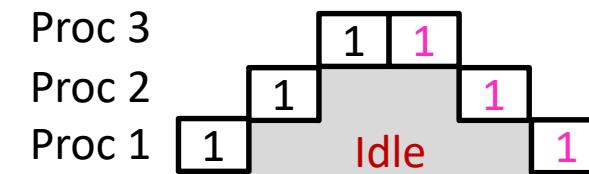
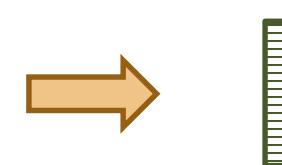
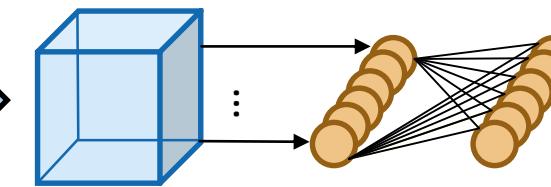
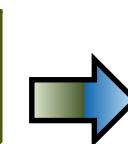
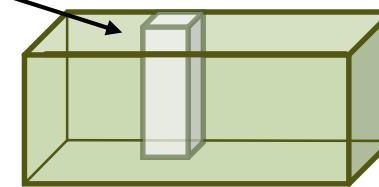
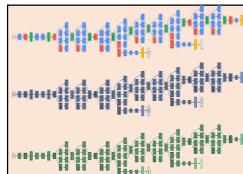
Machine Learning, and in particular Deep Learning [LeCun et al. 2015], is a field that is rapidly taking over a variety of aspects in our daily lives. In the core of deep learning lies the Deep Neural Network (DNN), a construct inspired by the interconnected nature of the human brain. Trained properly, the expressiveness of DNNs provides accurate solutions for problems previously thought to be unsolvable, simply by observing large amounts of data. Deep learning has been successfully implemented for a plethora of subjects, ranging from image classification [Huang et al. 2017], through speech recognition [Amodei et al. 2016] and medical diagnosis [Cireşan et al. 2013], to autonomous driving [Bojarski et al. 2016] and defeating human players in complex games [Silver et al. 2017] (see Fig. 1 for more examples).

Model parallelism – limited by network size



- Parameters can be distributed across processors
- Mini-batch has to be copied to all processors
- Backpropagation requires complex communication every layer

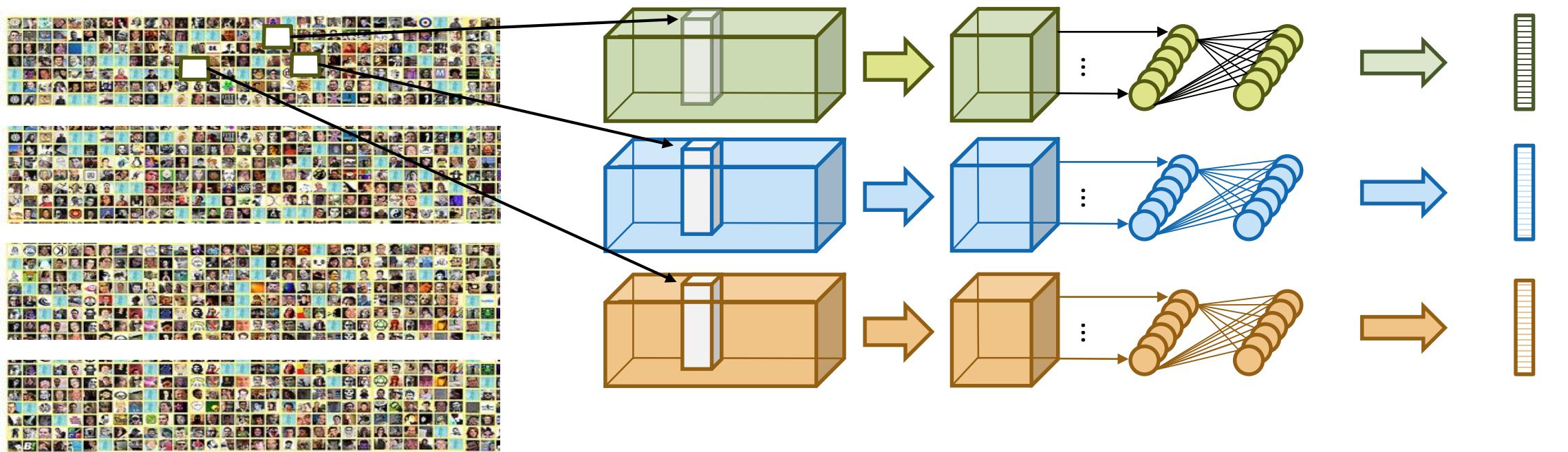
Pipeline parallelism – limited by network size



Microbatching

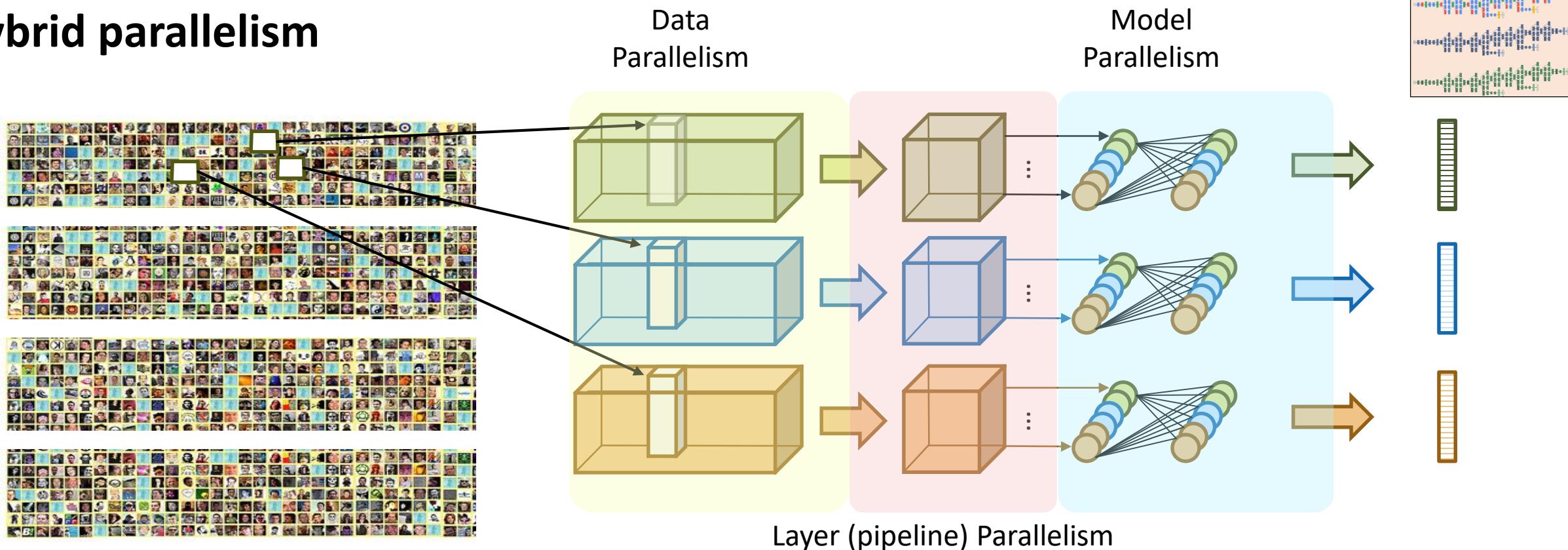
- Layers/parameters can be distributed across processors
- Sparse communication pattern (only pipeline stages)
- Mini-batch has to be copied through all processors
- Consistent model introduces idle-time “Bubble”

Data parallelism – limited by batch-size



- Simple and efficient solution, easy to implement
- Duplicate parameters at all processors
- Affects generalization

Hybrid parallelism



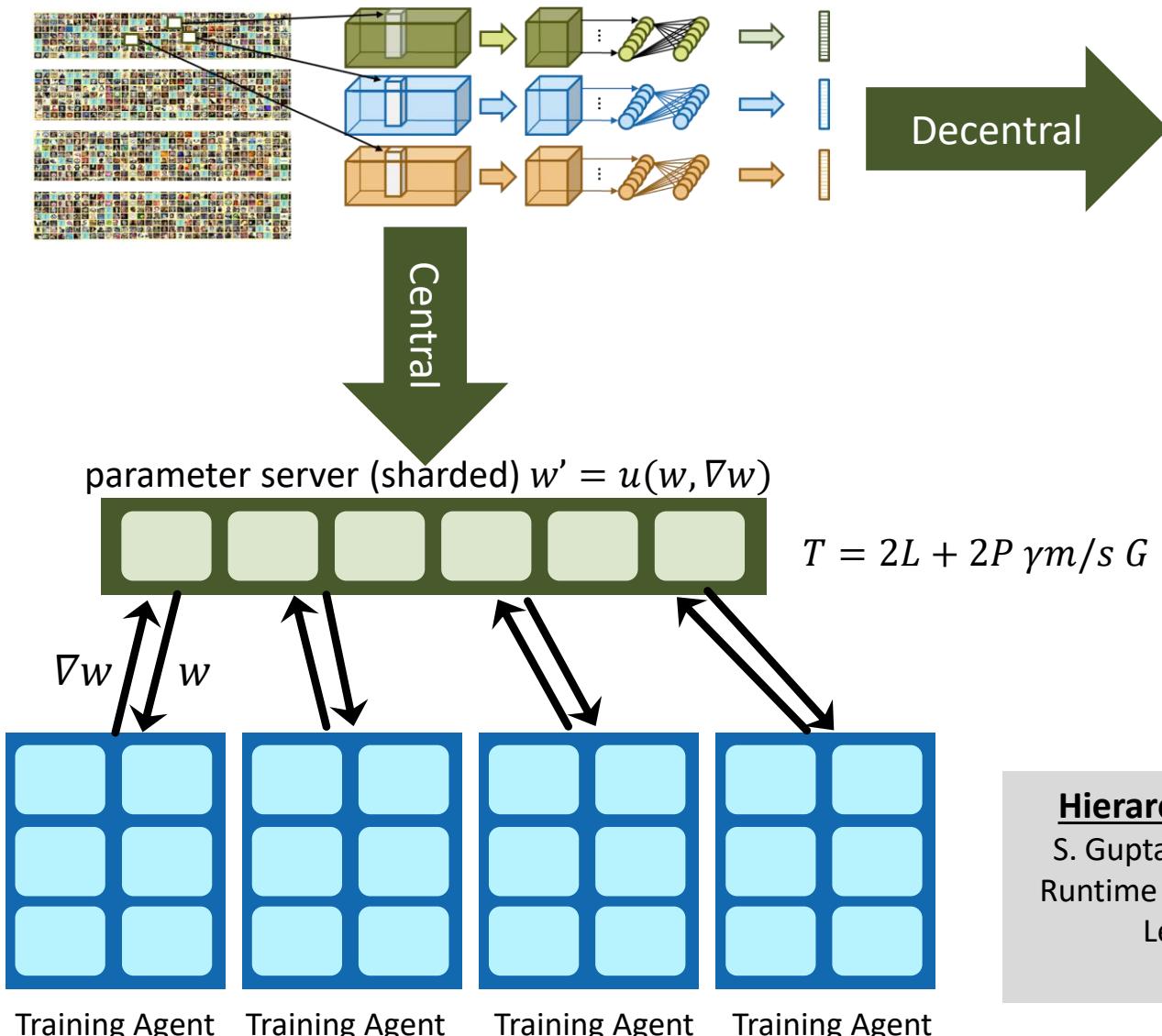
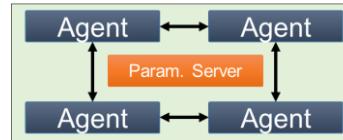
- Layers/parameters can be distributed across processors
- Can distribute minibatch
- Often specific to layer-types (e.g., distribute fc layers but handle conv layers data-parallel)
 - Enables arbitrary combinations of data, model, and pipeline parallelism – very powerful!

A. Krizhevsky: One weird trick for parallelizing convolutional neural networks, arXiv 2014

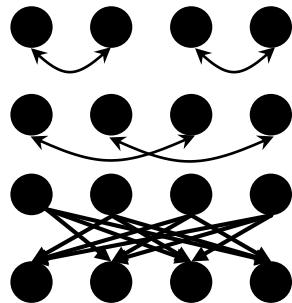
J. Dean et al.: Large scale distributed deep networks, NIPS'12.

T. Ben-Nun, T. Hoeefler: Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis, CSUR 2019

Updating parameters in **distributed** data parallelism



- Collective operations
- Topologies
- Neighborhood collectives
- RMA?



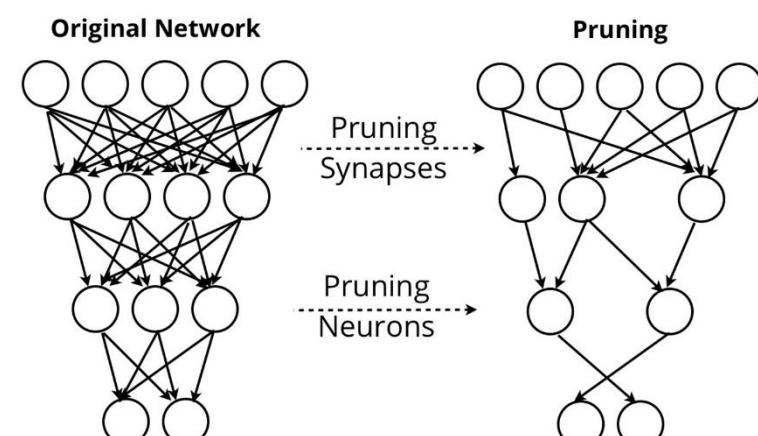
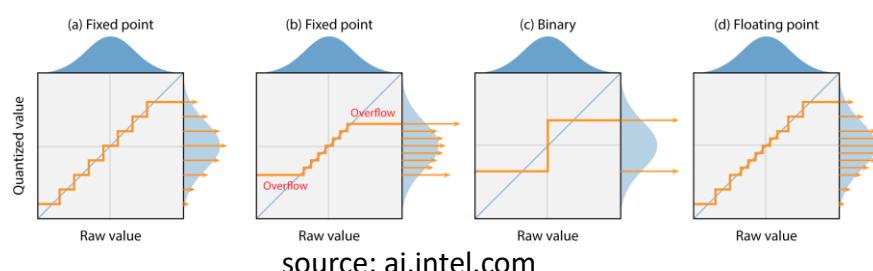
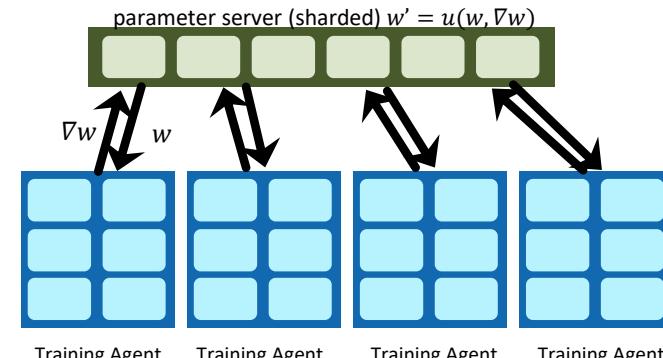
$$T = 2L \log_2 P + 2\gamma mG(P - 1)/P$$

Hierarchical Parameter Server
S. Gupta et al.: Model Accuracy and Runtime Tradeoff in Distributed Deep Learning: A Systematic Study. ICDM'16

Adaptive Minibatch Size
S. L. Smith et al.: Don't Decay the Learning Rate, Increase the Batch Size, arXiv 2017

Communication optimizations

- **Different options how to optimize updates**
 - Send ∇w , receive w
 - Send FC factors (o_{l-1}, o_l), compute ∇w on parameter server
Broadcast factors to not receive full w
 - Use lossy compression when sending, accumulate error locally!
- **Quantization**
 - Quantize weight updates and potentially weights
 - Main trick is stochastic rounding [1] – expectation is more accurate
Enables low precision (half, quarter) to become standard
 - TernGrad - ternary weights [2], 1-bit SGD [3], ...
- **Sparsification**
 - Do not send small weight updates **or** only send top-k [4]
Accumulate omitted gradients locally



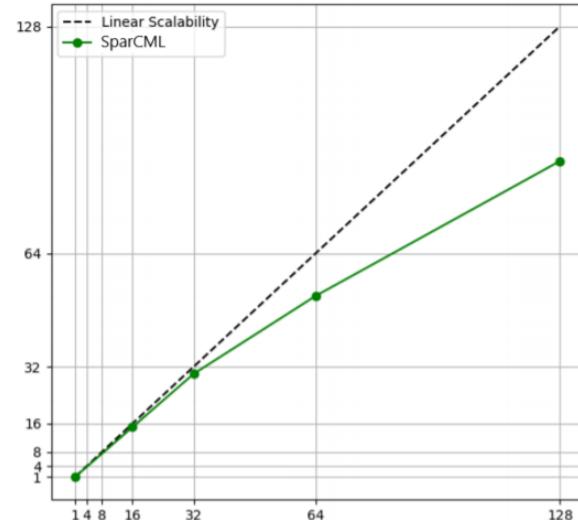
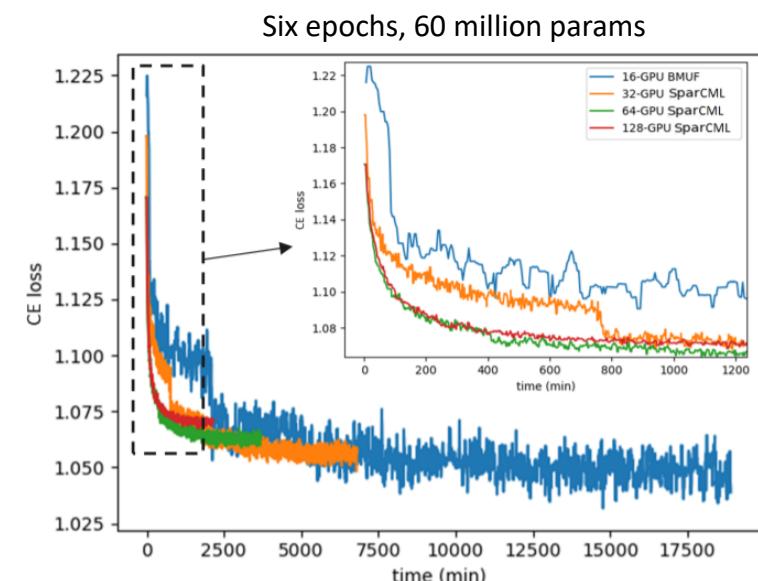
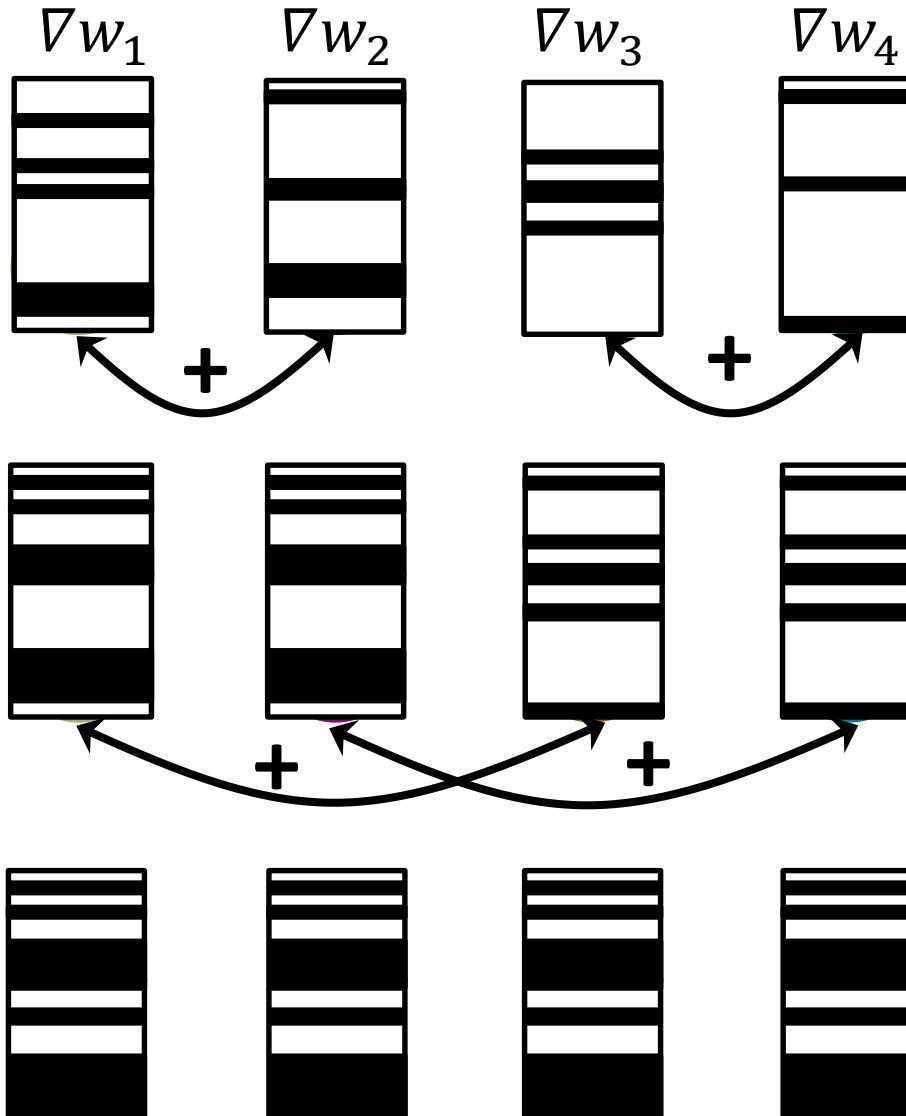
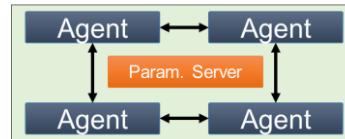
[1] S. Gupta et al. Deep Learning with Limited Numerical Precision, ICML'15

[2] F. Li and B. Liu. Ternary Weight Networks, arXiv 2016

[3] F. Seide et al. 1-Bit Stochastic Gradient Descent and Application to Data-Parallel Distributed Training of Speech DNNs, In Interspeech 2014

[4] C. Renggli et al. SparCML: High-Performance Sparse Communication for Machine Learning, arXiv 2018

SparCML – Quantized sparse allreduce for decentral updates



Microsoft Speech Production Workload Results – **2 weeks → 2 days!**

System	Dataset	Model	# of nodes	Algorithm	Speedup
Piz Daint	ImageNet	VGG19	8	Q4	1.55 (3.31)
Piz Daint	ImageNet	AlexNet	16	Q4	1.30 (1.36)
Piz Daint EC2	MNIST	MLP	8	Top16_Q4 Top16_Q4	3.65 (4.53) 19.12 (22.97)

Reproducing and Benchmarking Deep Learning

■ End result – generalization

Benchmark	Focus		Metrics										Criteria		Customizability			DL Workloads				Remarks		
	Perf	Con	Acc	Tim	Cos	Ene	Util	Mem	Tput	Brk	Sca	Com	TTA	FTA	Lat	Clo	Ope	Inf	Ops	Img	Obj	Spe	Txt	RL
DeepBench [39]	👍	👎	👎	👍	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👍	👍	👍	👍	👍	👎	👎	👎	👎	Ops: Conv., GEMM, RNN, Allreduce
TBD [47]	👍	👎	👎	👍	👎	👎	👍	👍	👍	👍	👎	👎	👍	👍	👍	👍	👎	👎	👍	👍	👍	👍	👍	+GANs
Fathom [2]	👍	👎	👎	👍	👎	👎	👎	👎	👍	👍	👍	👎	👍	👍	👍	👍	👎	👎	👍	👍	👍	👍	👍	+Auto-encoders
DAWNBench [9]	👍	👍	👎	👍	👍	👍	👎	👎	👎	👎	👎	👎	👎	👎	👍	👍	👎	👎	👍	👍	👎	👍	👍	👎
Kaggle [21]	👎	👎	👍	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👍	👍	👎	👎	👍	👍	👍	👍	👍	Varying workloads
ImageNet [13]	👎	👎	👍	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👍	👍	👎	👎	👎	👍	👍	👎	👎	👎
MLPerf [30]	👍	👍	👍	👍	👍	👍	👎	👍	👎	👎	👎	👎	👍	👍	👍	👍	👍	👎	👍	👍	👍	👍	👍	👍
Deep500	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍	👍

TABLE II: An overview of available DL benchmarks, focusing on the offered functionalities. **Perf**: Performance, **Con**: Convergence, **Acc**: Accuracy, **Tim**: Time, **Cos**: Cost, **Ene**: Energy, **Util**: Utilization, **Mem**: Memory Footprint, **Tput**: Throughput (Samples per Second), **Brk**: Timing Breakdown, **Sca**: Strong Scaling, **Com**: Communication and Load Balancing, **TTA**: Time to Accuracy, **FTA**: Final Test Accuracy, **Lat**: Latency (Inference), **Clo**: Closed (Fixed) Model Contests, **Ope**: Open Model Contests, **Inf**: Fixed Infrastructure for Benchmarking, **Ops**: Operator Benchmarks, **Img**: Image Processing, **Obj**: Object Detection and Localization, **Spe**: Speech Recognition, **Txt**: Text Processing and Machine Translation, **RL**: Reinforcement Learning Problems, **👍**: A given benchmark does offer the feature, **👎**: Planned benchmark feature, **👎**: A given benchmark does not offer the feature.

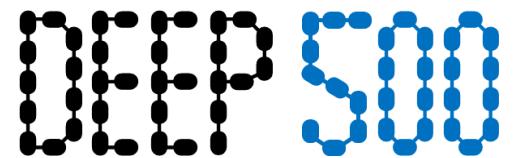
■ Sample throughput

Existing Deep Learning Frameworks

System	Operators		Networks		Training		Dist. Training						
	Sta	Cus	Def	Eag	Com	Tra	Dat	Opt	Cus	PS	Dec	Asy	Cus
(L) cuDNN	👍	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎
(L) MKL-DNN	👍	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎	👎
(F) TensorFlow [1]	👍	👍	👍	👍	👍	👍	UR	👍	👍	👍	👍	👍	👎
(F) Caffe, Caffe2 [†] [21]	👍	👍	👍	👎	👎	👎	UR	UR	👎	👎	👍	👎	👎
(F) [Py]Torch [†] [10, 35]	👍	👍	👎	👍	👎	👎	👍	👍	👍	👍	👍	👎	👎
(F) MXNet [6]	👍	👍	👍	👎	👎	👎	UR	UR	👍	👍	👍	👍	👎
(F) CNTK [48]	👍	👍	👍	👎	👎	👎	UR	UR	👍	👍	👍	👍	👎
(F) Theano [4]	👍	👍	👍	👍	👍	👍	UR	UR	👍	👎	👎	👎	👎
(F) Chainer[MN] [44]	👍	👍	👎	👍	👍	👍	UR	UR	👍	👍	👍	👍	👎
(F) Darknet [38]	👍	👎	👍	👎	👎	👎	UR	UR	👍	👎	👎	👎	👎
(F) DL4j [43]	👍	👍	👍	👎	👎	👎	UR	UR	👍	👍	👍	👍	👎
(F) DSSTNE	👍	👎	👍	👎	👎	👎	UR	UR	👍	👎	👎	👎	👎
(F) PaddlePaddle	👍	👍	👍	👎	👎	👎	UR	UR	👍	👍	👍	👍	👍
(F) TVM [7]	👍	👍	👍	👎	👍	👍	UR	UR	👍	👎	👎	👎	👎
(E) Keras [8]	👍	👎	👎	👎	👎	👎	UR	UR	👎	👎	👎	👎	👎
(E) Horovod [42]	👎	👎	👎	👎	👎	👎	UR	UR	👍	👍	👍	👍	👎
(E) TensorLayer [14]	👍	👎	👎	👎	👎	👎	UR	UR	👍	👍	👍	👍	👎
(E) Lasagne	👍	👍	👎	👎	👎	👎	UR	UR	👍	👎	👎	👎	👎
(E) TFLearn [11]	👍	👎	👎	👎	👎	👎	UR	UR	👍	👎	👎	👎	👎

- **Customizing operators** relies on framework
- **Network representation**
- **Dataset representation**
- **Training algorithm**
- **Distributed training (e.g., asynchronous SGD)**

Deep500



- Deep learning **meta-framework**: a framework for frameworks to reside in

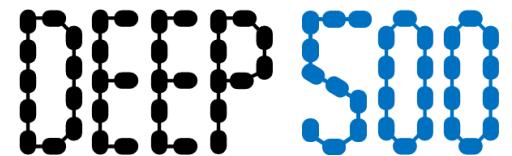
Level 0

forward()
gradient()



Operators

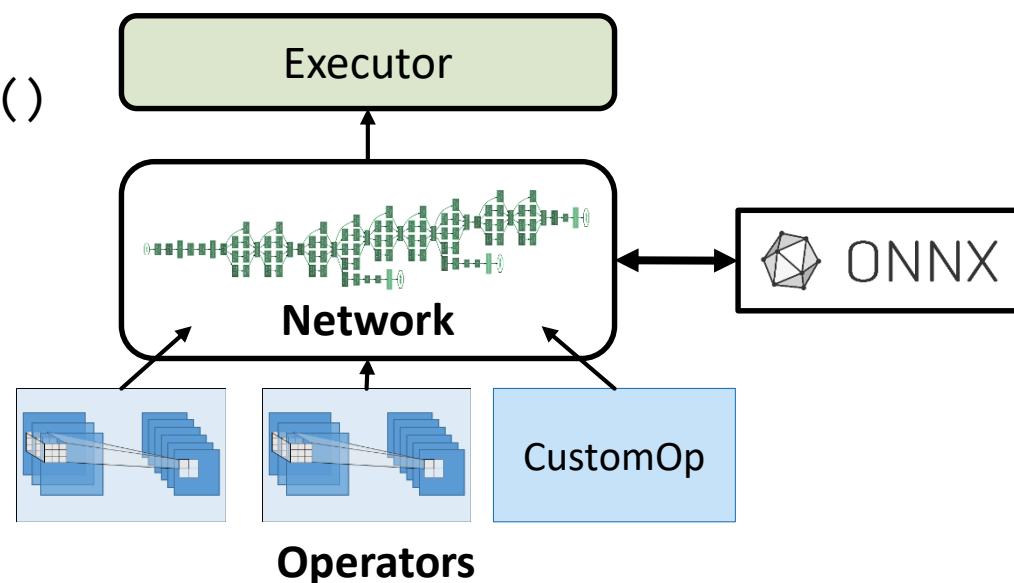
Deep500



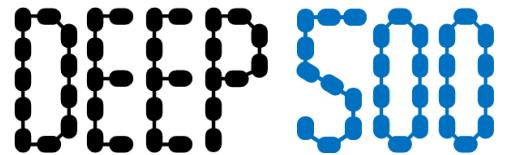
- Deep learning **meta-framework**: a framework for frameworks to reside in

`inference()`
`inference_and_backprop()`

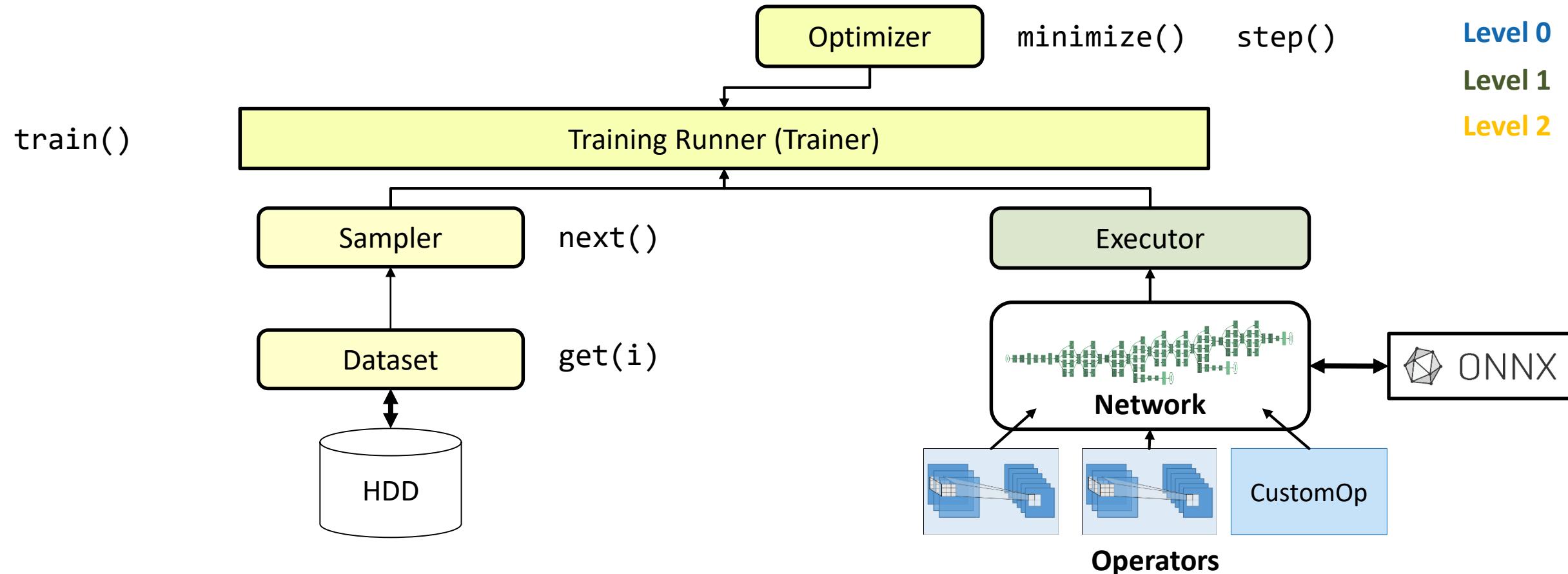
`add_node()`
`add_edge()`
`remove_...`



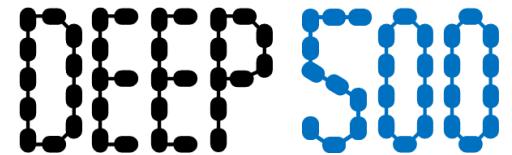
Deep500



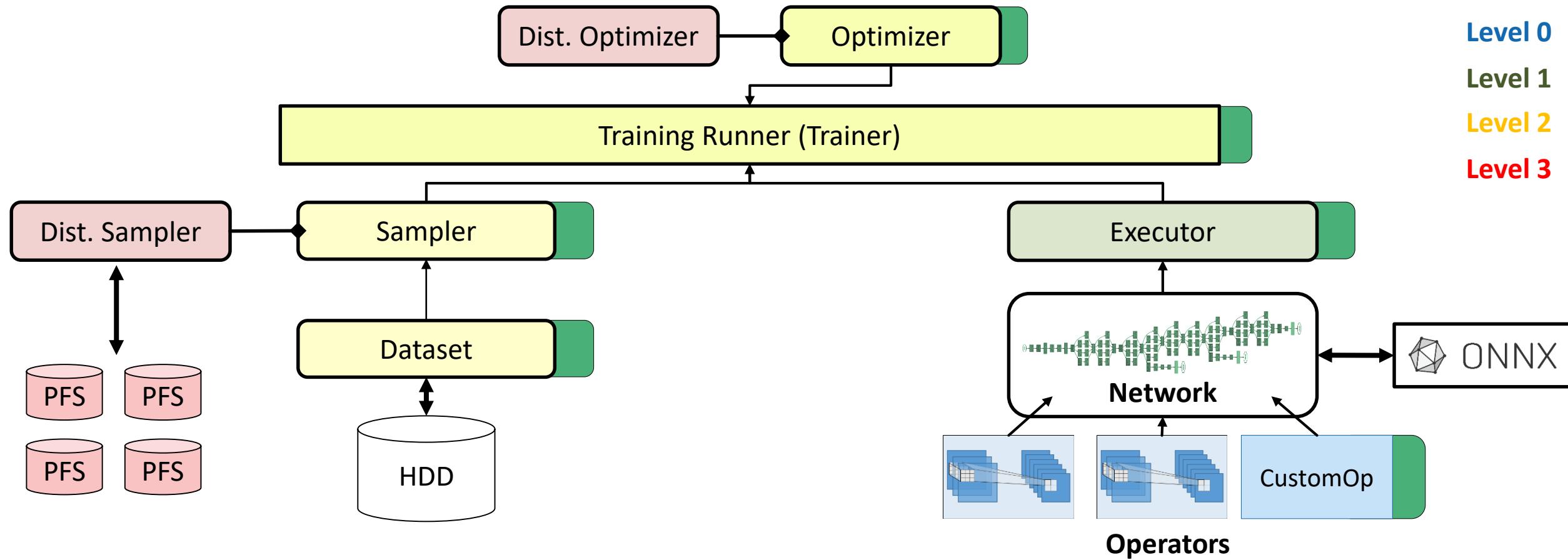
- Deep learning **meta-framework**: a framework for frameworks to reside in



Deep500



- Deep learning **meta-framework**: a framework for frameworks to reside in



For Benchmarking: Recipes

**Fixed definitions + mutable definitions +
acceptable metric set = Recipe**

For Benchmarking: Recipes

**Fixed definitions + mutable definitions +
acceptable metric set = Recipe**

```
1  """ A recipe for running the CIFAR-10 dataset with ResNet-44 and a momentum
2      optimizer, with metrics for final test accuracy. """
3
4  import deep500 as d5
5  from recipes.recipe import run_recipe
6
7 # Using PyTorch as the framework
8 import deep500.frameworks.pytorch as d5fw
9
10
11 # Fixed Components
12 FIXED = {
13     'model': 'resnet',
14     'model_kwarg': dict(depth=44),
15     'dataset': 'cifar10',
16     'train_sampler': d5.ShuffleSampler,
17     'epochs': 1
18 }
19
20 # Mutable Components
21 MUTABLE = {
22     'batch_size': 64,
23     'executor': d5fw.from_model,
24     'executor_kwarg': dict(device=d5.GPUDevice()),
25     'optimizer': d5fw.MomentumOptimizer,
26     'optimizer_args': (0.1, 0.9),
27 }
28
29 # Acceptable Metrics
30 METRICS = [
31     (d5.TestAccuracy(), 93.0)
32 ]
33
34
35 if __name__ == '__main__':
36     run_recipe(FIXED, MUTABLE, METRICS) or exit(1)
```

For Customizing: New Operator

```
class IPowOp(CustomPythonOp):
    def __init__(self, power):
        super(IPowOp, self).__init__()
        self.power = power
        assert int(power) == power # integral

    def forward(self, inputs):
        return inputs[0] ** self.power

    def backward(self, grads, fwd_inputs, fwd_outputs):
        return (grads[0] * self.power *
               (fwd_inputs[0] ** (self.power - 1)))
```

Python

```
template<typename T>
class ipowop : public deep500::CustomOperator {
protected:
    int m_len;
public:
    ipowop(int len) : m_len(len) {}
    virtual ~ipowop() {}

    void forward(const T *input, T *output) {
        #pragma omp parallel for
        for (int i = 0; i < m_len; ++i)
            output[i] = std::pow(input[i], DPOWER);
    }

    void backward(const T *nextop_grad,
                 const T *fwd_input_tensor,
                 const T *fwd_output_tensor,
                 T *input_tensor_grad) {
        #pragma omp parallel for
        for (int i = 0; i < m_len; ++i) {
            input_tensor_grad[i] = nextop_grad[i] * DPOWER *
                std::pow(fwd_input_tensor[i], DPOWER - 1);
        }
    }
};
```

C++

For Customizing: Distributed Optimization

```
class ConsistentNeighbors(DistributedOptimizer):  
    # Follows communication scheme from https://arxiv.org/pdf/1705.09056.pdf  
  
    def step(self, inputs):  
        self.base_optimizer.new_input()  
        for param in self.network.get_params():  
            self.base_optimizer.prepare_param(param)  
        output = self.executor.inference_and_backprop(inputs, self.base_optimizer.loss)  
        gradients = self.network.gradient(self.base_optimizer.loss)  
        for param_name, grad_name in gradients:  
            param, grad = self.network.fetch_tensors([param_name, grad_name])  
            grad = self.communication.reduce_from_neighbors(grad) / 3  
            param = self.base_optimizer.update_rule(grad, param, param_name)  
            self.network.feed_tensor(param_name, param)  
    return output
```

HPC for Deep Learning – Summary

- A supercomputing problem - amenable to established tools and tricks from HPC
- Concurrency is easy to attain, hard to program beyond data-parallelism
- Main bottleneck in distributed is communication – reduction by using the robustness of SGD
- Co-design is prevalent
- Very different environment from traditional HPC
 - Trade-off accuracy for performance!
- Main objective is generalization
 - Performance-centric view in HPC can be harmful for accuracy

<https://www.arxiv.org/abs/1802.09941>

1

Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis

TAL BEN-NUN^{*} and TORSTEN HOEFLER, ETH Zurich

Deep Neural Networks (DNNs) are becoming an important tool in modern computing applications. Accelerating their training is a major challenge and techniques range from distributed algorithms to low-level circuit design. In this survey, we describe the problem from a theoretical perspective, followed by approaches for its parallelization. Specifically, we present trends in DNN architectures and the resulting implications on parallelization strategies. We discuss the different types of concurrency in DNNs; synchronous and asynchronous stochastic gradient descent; distributed system architectures; communication schemes; and performance modeling. Based on these approaches, we extrapolate potential directions for parallelism in deep learning.

CCS Concepts: • General and reference → Surveys and overviews; • Computing methodologies → Neural networks; Distributed computing methodologies; Parallel computing methodologies; Machine learning;

Additional Key Words and Phrases: Deep Learning, Distributed Computing, Parallel Algorithms

ACM Reference format:

Tal Ben-Nun and Torsten Hoefler. 2018. Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis. 60 pages.

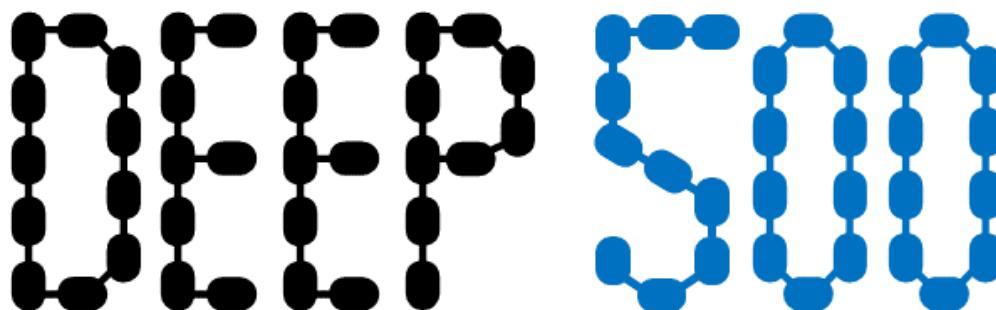
1 INTRODUCTION

Machine Learning, and in particular Deep Learning [LeCun et al. 2015], is a field that is rapidly taking over a variety of aspects in our daily lives. In the core of deep learning lies the Deep Neural Network (DNN), a construct inspired by the interconnected nature of the human brain. Trained properly, the expressiveness of DNNs provides accurate solutions for problems previously thought to be unsolvable, simply by observing large amounts of data. Deep learning has been successfully implemented for plethora of subjects, ranging from image classification [Huang et al. 2017], through speech recognition [Amodei et al. 2016] and medical diagnosis [Cireşan et al. 2013], to autonomous driving [Bojarski et al. 2016] and defeating human players in complex games [Silver et al. 2016].

Next steps – Community!

- More recipes
- More datasets (scientific computing)
- Use concepts from HPC to improve ML
 - Better formats
 - Communication schemes
- Implement reproducible methods
- Metrics and aggregate scores

<https://www.deep500.org/>
<https://www.github.com/deep500/deep500>



A Modular Benchmarking Infrastructure for High-Performance and Reproducible Deep Learning

Tal Ben-Nun, Maciej Besta, Simon Huber, Alexandros Nikolaos Zygias, Daniel Peter, Torsten Hoefer
Department of Computer Science, ETH Zurich

Abstract—We introduce Deep500: the first customizable benchmarking infrastructure that enables fair comparison of the plethora of deep learning frameworks, algorithms, libraries, and tools. The key idea behind Deep500 is its **modular** design, where deep learning is factorized into four distinct **operator**s: operators, network processing, training, and distributed training. Our evaluation illustrates that Deep500 is **customizable** (enables configuration and benchmarking of deep learning codes) and **fair** (uses automatically selected metrics). Moreover, Deep500 is **fast** (incurs negligible overheads), **verifiable** (offers infrastructure to analyze correctness), and **reproducible**. Finally, as the first distributed and reproducible benchmarking system for deep learning, Deep500 provides software infrastructure to utilize the most powerful supercomputers for extreme-scale workloads.

Index Terms—Distributed Deep Learning, High-Performance Deep Learning, Parallel Deep Learning, Benchmarking

Deep500 Code: <https://github.com/deep500/deep500>

I. INTRODUCTION
 Deep Learning (DL) has transformed the world and is now ubiquitous in areas such as speech recognition, image classification, or autonomous driving [1]. Its central concept is a Deep Neural Network (DNN), a structure modeled after the human brain. Thanks to rigorous training, DNNs are able to solve various problems previously deemed unsolvable.

Recent years saw an unprecedented growth in the number of approaches, schemes, algorithms, applications, platforms, and frameworks for DL. First, DL computations can aim at inference, training, or distributed training. Inference is significantly more complex than training. Training, for example, can be computed using different methods, e.g., im2col [2] or Winograd [3] in convolutions. Next, DL functionalities have been deployed in a variety of frameworks, such as TensorFlow [4] or Caffe [5]. These functionalities may incorporate many parallel and distributed optimizations, such as data, model, and pipeline parallelism. Finally, DL workloads are executed in wildly varying environments, such as mobile phones, multi-GPU clusters, or large-scale supercomputers.

This richness of the DL domain raises an important question: How can we enable a level playing ground for comparison, configuration, and benchmarking of Deep Learning? The key issue is that, due to the complex nature of DL workloads, there is no single metric by which one DNN or hardware is objectively better than another on all counts. This

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System	Operators	Networks	Training	Distr. Training	Sta	Cus	Def	Esg	Com	Trn	Dst	Opt	Cus	PS	Dec	Asy
(I) ML-DNN																
(II) ML-DNN																
(III) TensorFlow [6]	TensorFlow [6]				TensorFlow [6]											
(IV) Caffe, Caffe2 [5]	Caffe, Caffe2 [5]				Caffe, Caffe2 [5]											
(V) MNNet [9]	MNNet [9]				MNNet [9]											
(VI) Theano [11]	Theano [11]				Theano [11]											
(VII) Chainer/MxNet [12]	Chainer/MxNet [12]				Chainer/MxNet [12]											
(VIII) DL4J [14]	DL4J [14]				DL4J [14]											
(IX) PaddlePaddle	PaddlePaddle				PaddlePaddle											
(X) TVM [15]	TVM [15]				TVM [15]											
(XI) Keras [16]	Keras [16]				Keras [16]											
(XII) PyTorch [17]	PyTorch [17]				PyTorch [17]											
(XIII) TensorFlow.js [4]	TensorFlow.js [4]				TensorFlow.js [4]											
(XIV) TensorFlow Lite [18]	TensorFlow Lite [18]				TensorFlow Lite [18]											

TABLE I: An overview of DL frameworks, libraries, and systems that can be integrated within Deep500. This work